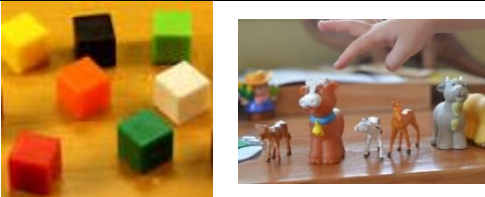

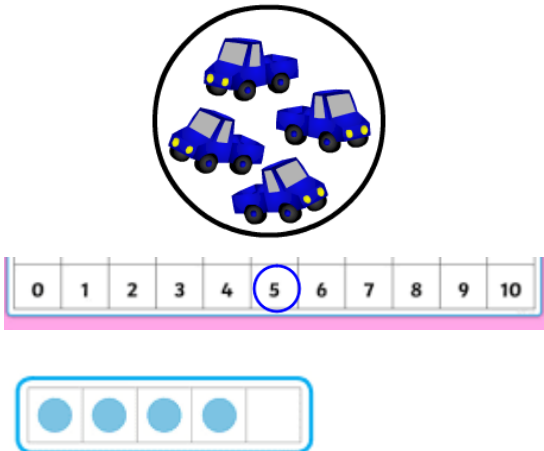
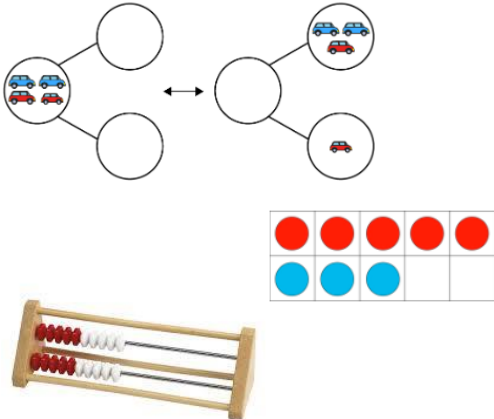
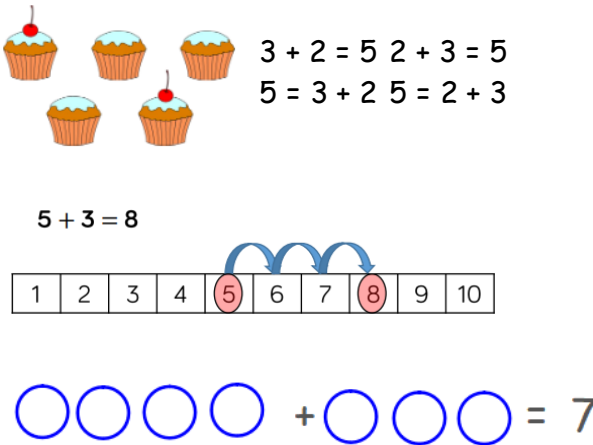
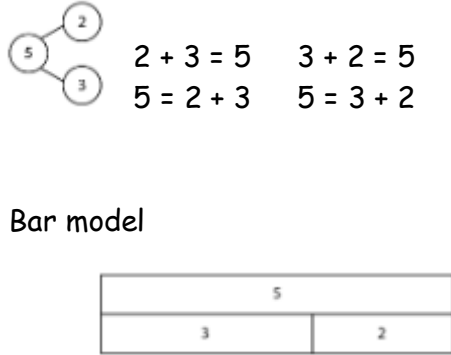




CALCULATION POLICY

January 2023

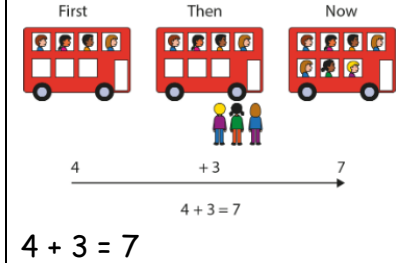
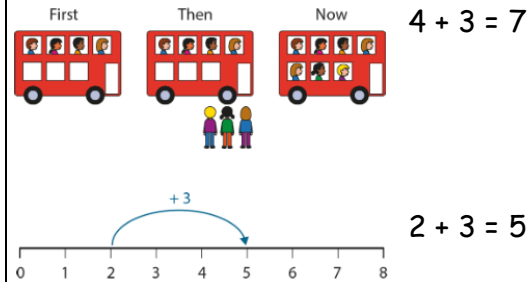
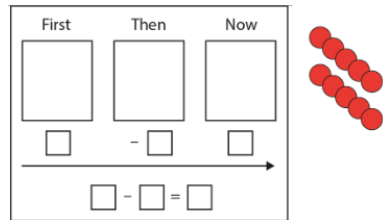
Addition

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)										
<p>Can you show me ____?</p> <p>____ is ____ and one more.</p> <p>EYFS</p>	 		<table border="1" data-bbox="1769 287 2038 595"><tr><td></td><td>3</td></tr><tr><td></td><td>5</td></tr><tr><td></td><td>1</td></tr><tr><td></td><td>2</td></tr><tr><td></td><td>4</td></tr></table> <p>Children relate the number of objects to the numeral.</p>		3		5		1		2		4
	3												
	5												
	1												
	2												
	4												
<p>____ is the whole, ____ is a part, ____ is a part.</p> <p>____ = ____ plus ____ and ____ plus ____ = ____</p> <p>There are ____ in total.</p> <p>EYFS/1</p>			 <p>Bar model</p>										

First... Then... Now...
e.g. **First** there were 4 children on the bus, **then** 3 children got on. **Now** there are 7 children on the bus.

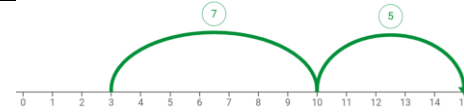
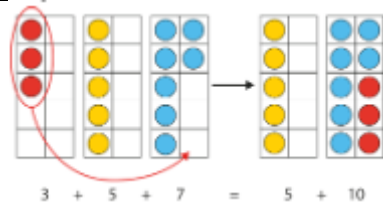
EYFS/1

Role play getting 'on the bus' or use a toy bus.

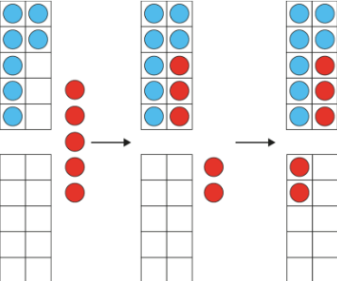

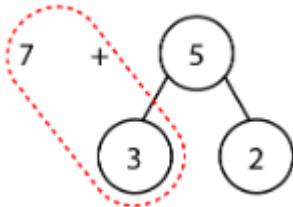
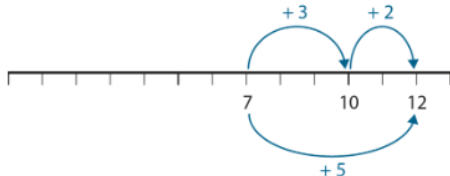
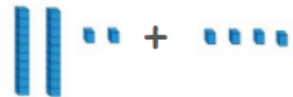





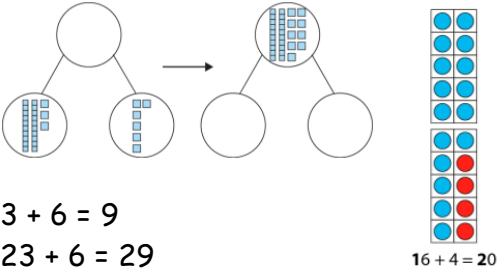
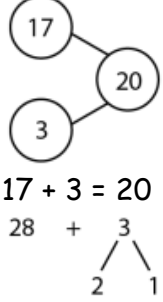
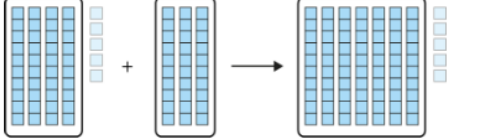
We can look for pairs of numbers which sum to 10.
___ plus ___ is equal to 10,
then 10 plus ___ is equal to ___.

Year 1/2



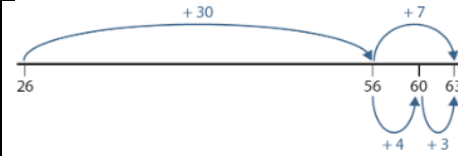
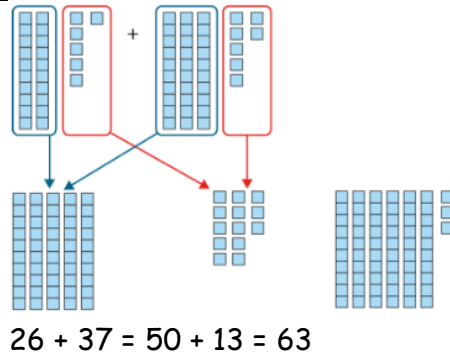
$$3 + 5 + 7 = 10 + 5 = 15$$

<p>First I partition the __: __ plus __ is equal to __. Then __ plus __ is equal to ten ... and ten plus __ is equal to __.</p> <p>Year 1/2</p>	 <p> $7 + 5 =$ $7 + 3 = 10$ $10 + 2 = 12$ </p> 	 	<p> $7 + 3 = 10$ $10 + 2 = 12$ </p> <p> $7 + 5 =$ $7 + 3 + 2 = 10 + 2$ $10 + 2 = 12$ </p>
<p>Year 1/2</p>			<p>$22 + 4 = 26$</p>
<p>First I partition the __ into __ and __, and the __ into __ and __. __ plus __ is equal to __... (addition of the tens) __ plus __ is equal to __... (addition of the ones) and __ plus __ is equal to __. (addition of the tens and ones) So __ plus __ is equal to __. (summary of the overall calculation)</p>			<p>$34 + 23 = 57$</p>

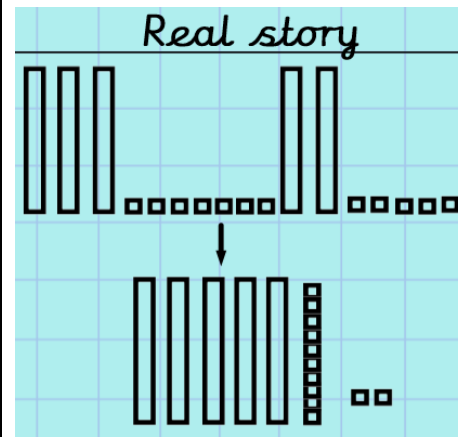
<p>Year 1/2</p>			
<p>I know that ___ plus ___ is equal to ___. (single-digit fact) So ___ plus ___ is equal to ___. (related two-digit plus single digit fact) I know that ___ plus ___ is equal to ten so ___ plus ___ is equal to ___. Year 1/2</p>	 <p> $3 + 6 = 9$ $23 + 6 = 29$ $16 + 4 = 20$ </p>	<p> $3 + 6 = 9$ $23 + 6 = 29$ </p>	 <p> $17 + 3 = 20$ $28 + 3 = 31$ </p>
<p>I know that ___ plus ___ is equal to ___. So ___ tens plus ___ tens is equal to ___ tens. ___ tens and ___ ones, plus ___ tens is equal to ___ tens and ___ ones. Year 2</p>	 <p> $40 + 30 = 70$ so $45 + 30 = 75$ </p>	<p> $45 + 30 = 75$ </p>	<p> $4 + 3 = 7$ $4 \text{ tens} + 3 \text{ tens} = 7 \text{ tens}$ $40 + 30 = 70$ So $45 + 30 = 75$ </p>

First I partition the __ into __ and __, and the __ into __ and __.
 __ plus __ is equal to ____
 (addition of the tens)
 __ plus __ is equal to ____
 (addition of the ones)
 and __ plus __ is equal to __.
 (addition of the tens and ones)
 So __ plus __ is equal to __.
 (summary of the overall calculation)

Year 2



$26 + 30 = 56$
 $56 + 7 = 63$



$37 + 25 = 62$

$26 + 37$ or $26 + 37$
 $20 \ 6 \ 30 \ 7 \ 30 \ 7$

$20 + 30 = 50$
 $6 + 7 = 13$
 $50 + 13 = 63$

$26 + 30 = 56$
 $56 + 7 = 63$

Addition Facts

Adding 1

Bonds to 10

Adding 10

Bridging/compensating

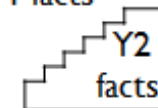
Adding 2

Adding 0

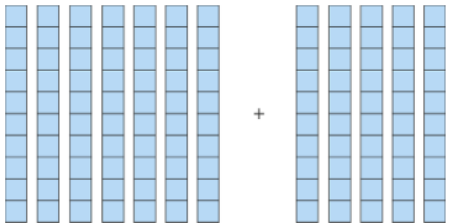
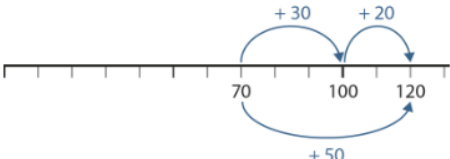
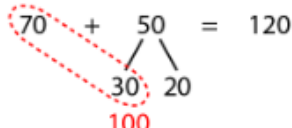
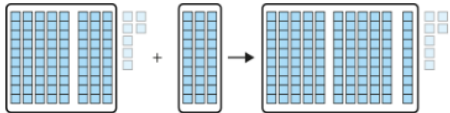
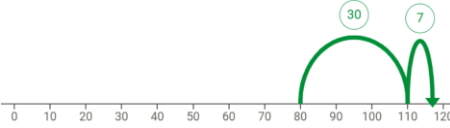
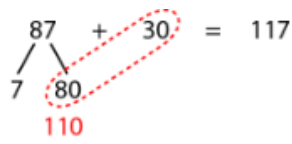
Doubles

Near doubles

Y1 facts



+	0	1	2	3	4	5	6	7	8	9	10
0	0 + 0	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5	0 + 6	0 + 7	0 + 8	0 + 9	0 + 10
1	1 + 0	1 + 1	1 + 2	1 + 3	1 + 4	1 + 5	1 + 6	1 + 7	1 + 8	1 + 9	1 + 10
2	2 + 0	2 + 1	2 + 2	2 + 3	2 + 4	2 + 5	2 + 6	2 + 7	2 + 8	2 + 9	2 + 10
3	3 + 0	3 + 1	3 + 2	3 + 3	3 + 4	3 + 5	3 + 6	3 + 7	3 + 8	3 + 9	3 + 10
4	4 + 0	4 + 1	4 + 2	4 + 3	4 + 4	4 + 5	4 + 6	4 + 7	4 + 8	4 + 9	4 + 10
5	5 + 0	5 + 1	5 + 2	5 + 3	5 + 4	5 + 5	5 + 6	5 + 7	5 + 8	5 + 9	5 + 10
6	6 + 0	6 + 1	6 + 2	6 + 3	6 + 4	6 + 5	6 + 6	6 + 7	6 + 8	6 + 9	6 + 10
7	7 + 0	7 + 1	7 + 2	7 + 3	7 + 4	7 + 5	7 + 6	7 + 7	7 + 8	7 + 9	7 + 10
8	8 + 0	8 + 1	8 + 2	8 + 3	8 + 4	8 + 5	8 + 6	8 + 7	8 + 8	8 + 9	8 + 10
9	9 + 0	9 + 1	9 + 2	9 + 3	9 + 4	9 + 5	9 + 6	9 + 7	9 + 8	9 + 9	9 + 10
10	10 + 0	10 + 1	10 + 2	10 + 3	10 + 4	10 + 5	10 + 6	10 + 7	10 + 8	10 + 9	10 + 10

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>I know that __ plus __ is equal to __. (single-digit numbers)</p> <p>So __ tens plus __ tens is equal to __ tens. (multiple-of-ten numbers)</p> <p>__ plus __ is equal to one hundred and __.</p> <p>Year 3</p>	 <p>7 + 5 = 12 7 tens + 5 tens = 12</p> <p>tens 70 + 50 = 120</p>		 <p>70 + 50 = 70 + 30 + 20 = 100 + 20 = 120</p>
<p>I know that __ plus __ is equal to __. (single-digit numbers)</p> <p>So __ tens plus __ tens is equal to __ tens. (multiple-of-ten numbers)</p> <p>__ plus __ is equal to one hundred and __.</p> <p>Year 3</p>	 <p>87 + 30 = 110 + 7 = 117</p>		 <p>87 + 30 = 80 + 7 + 30 = 110 + 7 = 117</p>

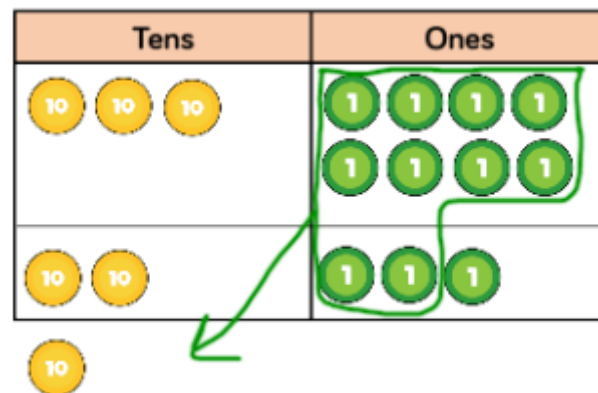
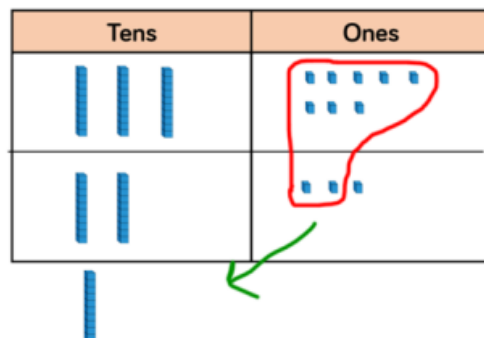
We line up the ones; ___ ones plus ___ ones.
 We line up the tens; ___ tens plus ___ tens.
 The ___ is in the ones column – it represents ___ ones. The ___ is in the ones column – it represents ___ ones.
 ___ ones plus ___ ones is equal to ___ ones.
 The ___ is in the tens column – it represents ___ tens. The ___ is in the tens column – it represents ___ tens.
 ___ tens plus ___ tens is equal to ___ tens.

In column addition we start at the right-hand side.

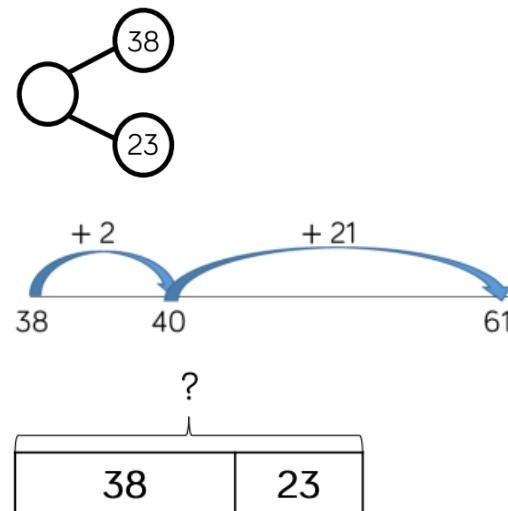
If the column sum is equal to ten or more, we must regroup.

Year 3

Start with two-digit numbers to exemplify lining up the columns.



Children could draw place value counters or the diennes concrete materials.



Start with two-digit numbers to exemplify lining up the columns.

$$38 + 23 = 61$$

$$\begin{array}{r} 38 \\ + 23 \\ \hline 61 \\ \hline 1 \end{array}$$

If the column sum is equal to ten or more, we must regroup.

Year 4

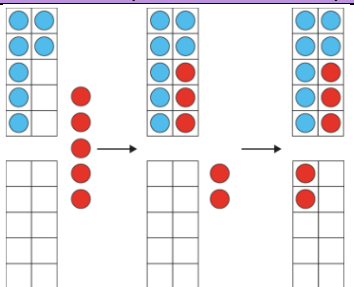
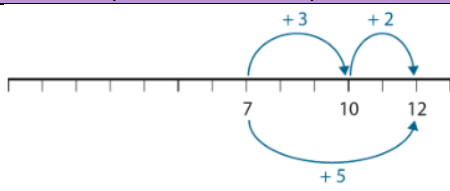
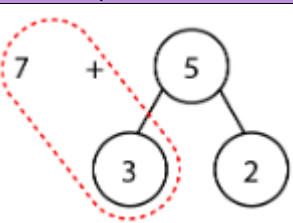

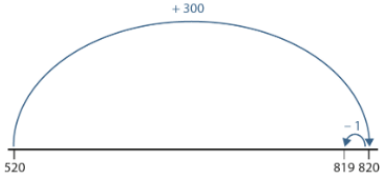
See Year 3 examples

See Year 3 examples

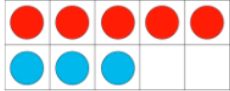
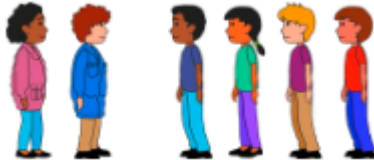

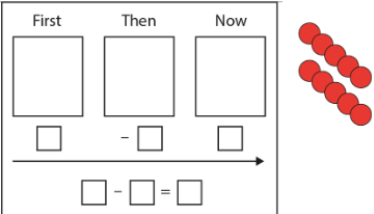
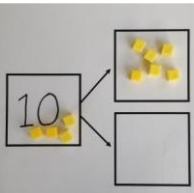
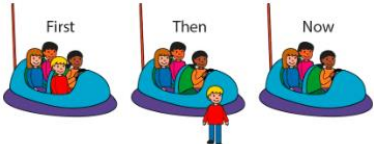
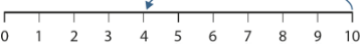
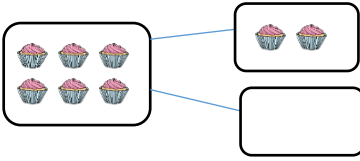
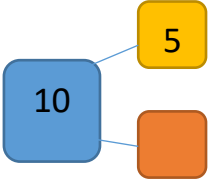
$$\begin{array}{r} 6, 5 \ 8 \ 4 \\ + \ 2, 7 \ 3 \ 9 \\ \hline 9, 3 \ 2 \ 3 \\ \hline 1 \ 1 \ 1 \end{array}$$

			$ \begin{array}{r} £ 24.55 \\ + £ 17.82 \\ \hline £ 42.37 \\ \hline 11 \end{array} $
<p>If the column sum is equal to ten or more, we must regroup.</p> <p>Years 5 and 6</p>	See Year 3 examples	See Year 3 examples	As in Year 4 but using numbers with more than 4 digits

Addition – Key mental strategies for Key Stage 2

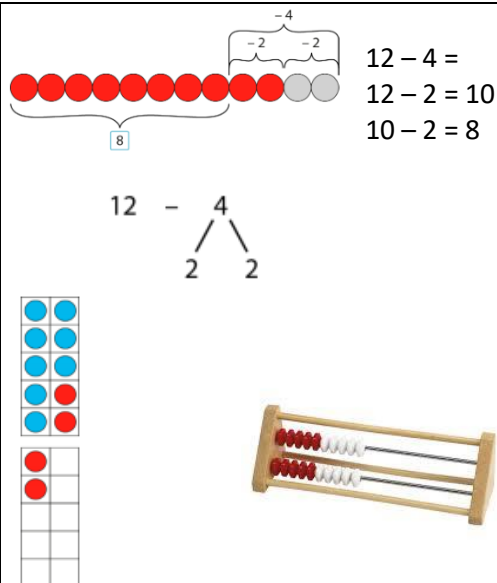
Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>Bridging through a multiple of 10, 100, etc</p> <p>Years 3, 4, 5 and 6</p>	 <p> $7 + 5 =$ $7 + 3 = 10$ $10 + 2 = 12$ </p>	 <p> $7 + 5 =$ $7 + 3 = 10$ $10 + 2 = 12$ </p>	 <p> $7 + 3 = 10$ $10 + 2 = 12$ </p>
<p>Compensating – rounding to the nearest multiple 10, 100, etc and adjusting</p> <p>Years 3, 4, 5 and 6</p>	 <p>$35 + 49 = 34 + 50 = 84$</p>	 <p> $520 + 299 =$ $520 + 300 = 820$ $820 - 1 = 819$ </p>	<p> $69 + 69 = \boxed{138}$ </p> <p> $70 + 70 = \boxed{140}$ </p> <p>← -2</p>

Subtraction

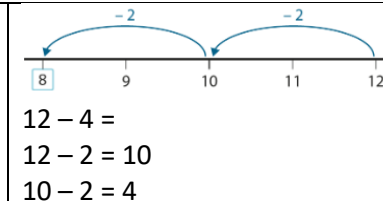
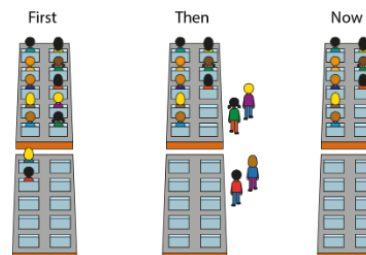
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>___ is the whole, ___ is a part, ___ is a part.</p> <p>___ = ___ minus ___ and ___ minus ___ = ___</p> <p>Year R/1</p>	<p>I have 8 counters. 5 counters are red. How many are blue?</p> 	<p>There are 6 children. 2 have their coat on. How many do not have their coat on?</p> 	<p>There are 8 flowers. 2 are red and the rest are yellow. How many are yellow?</p>  <p>$8 - 2 = 6$</p>
<p>First... Then... Now...</p> <p>e.g. First there were 4 children in the car, then 1 child got out. Now there are 3 children in the car.</p> <p>Year R/1</p>	<p>Role play 'getting out of a car'.</p>  <p>Link to addition – use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is the part. What is the other part?</p> 	<p>First Then Now</p>  <p>$4 - 1 = 3$ $3 = 4 - 1$</p> <p>Start with the whole and count back the part showing the jumps on the number line</p>  <p>$10 - 6 = 4$</p> <p>Use a pictorial representation of objects to show the part whole model.</p> 	<p>If you know that $5 + 5 = 10$ Then you also know that $10 - 5 = 5$</p> <p>Move to using numbers within the part whole model.</p> 

We partition the into and .
 First we subtract the from to get to 10.
 Then we subtract the remaining from 10.
 We know 10 minus is equal to .

Year 2

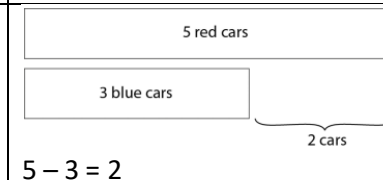
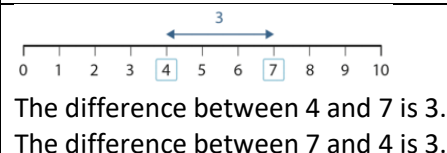
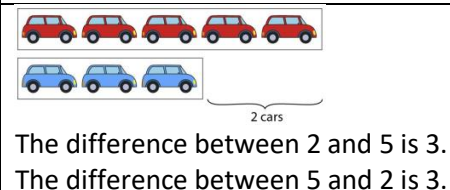


First there were 12 children on the ride.
 Then 4 got off. Now there are 8 children on the ride.



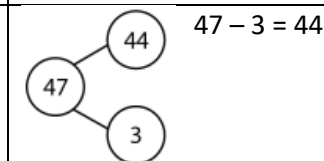
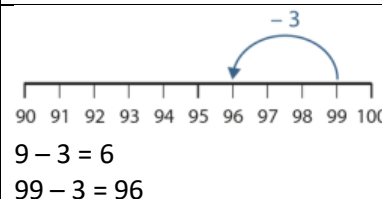
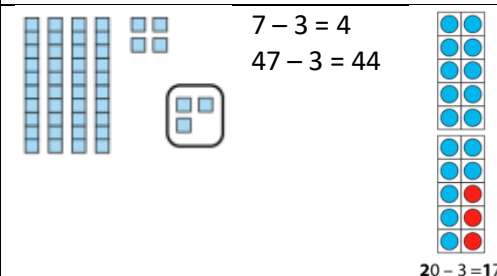
There are more than .
 There are fewer than .
 The difference between and is .

Year 2



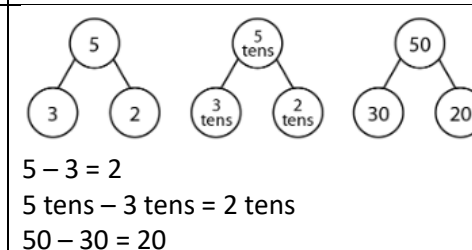
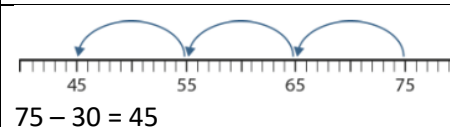
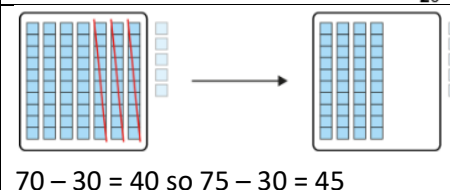
I know that minus is equal to .
 (single-digit fact)
 So minus is equal to . (related two-digit minus single digit fact)
 I know that ten minus is equal to so minus is equal to .

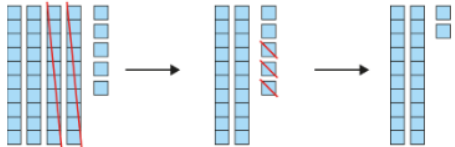
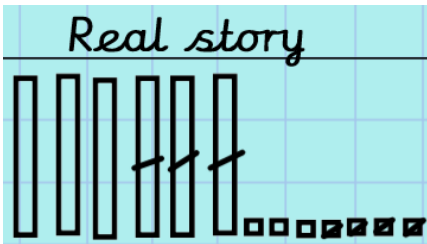
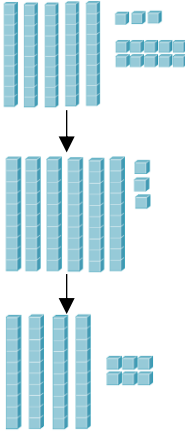
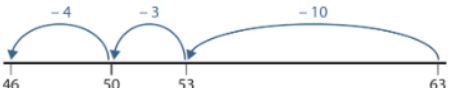
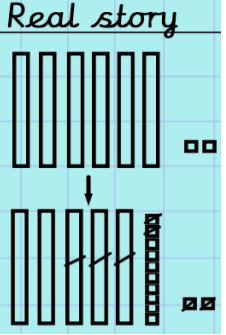
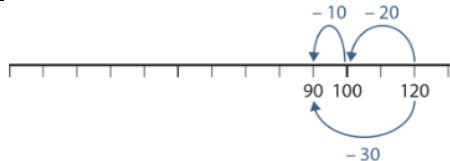
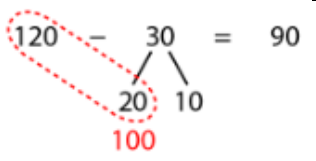

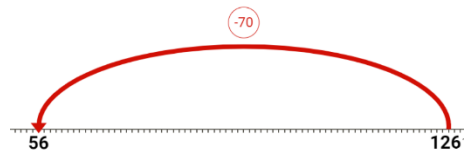
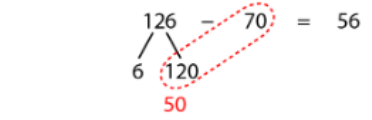
Year 2

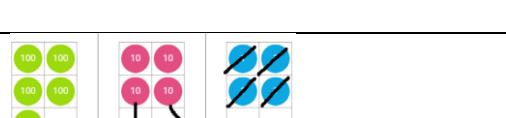
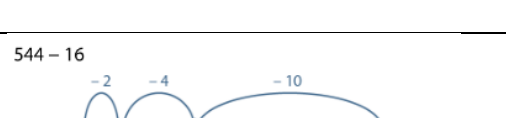
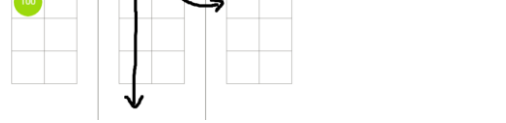



I know that minus is equal to .
 So tens minus tens is equal to tens.

Year 2

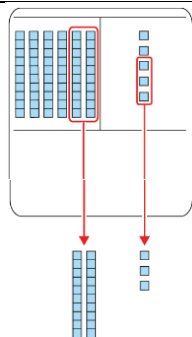


<p>First I subtract the tens, then I subtract the ones.</p> <p>Year 2</p>	 $45 - 23 =$ $45 - 20 = 25$ $25 - 3 = 22$	$67 - 34 = 33$ 	$45 - 23 = 22$
<p>First I subtract the tens, then I subtract the ones.</p> <p>Year 2</p>		 <p><i>Real story</i></p>  $62 - 34 = 28$	$63 - 17 = 46$
<p>I know that ___ minus ___ is equal to ___. (bridging ten) So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens) One hundred and ___ minus ___ is equal to ___.</p> <p>Year 3</p>	<p>See Year 2 (bridging)</p>	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$
<p>I know that ___ minus ___ is equal to ___. (bridging ten) So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens) One hundred and ___ minus ___ is equal to ___.</p> <p>Year 3</p>	 $126 - 70 = 56$		 $126 - 70 = 120 - 70 + 6$ $= 50 + 6$ $= 56$

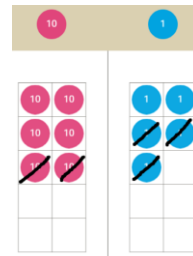
<p>We partition the <u> </u> into <u> </u> and <u> </u>. First we subtract the <u> </u> from <u> </u> to get to a multiple of 10. Then we subtract the remaining <u> </u> from the multiple of 10. We know 10 minus <u> </u> is equal to <u> </u> so <u> </u> minus <u> </u> is equal to <u> </u>.</p> <p>Year 3</p>		<p>544 – 16</p> 	<p>Count back to multiples of 10/100</p>
<p>We partition the <u> </u> into <u> </u> and <u> </u>. First we add the <u> </u> to <u> </u> to get to 100. Then we add the remaining <u> </u> to 100. We know 100 plus <u> </u> is equal to <u> </u>.</p> <p>Year 3</p>		<p>123 – 97 = 26</p> 	<p>Count on to multiples of 10/100</p>

We line up the ones; ___ ones plus ___ ones.
 We line up the tens: ___ tens plus ___ tens.
 The ___ is in the ones column – it represents ___ ones.
 ___ ones minus ___ ones is equal to ___ ones.
 The ___ is in the tens column – it represents ___ tens.
 ___ tens minus ___ tens is equal to ___ tens.
 In column subtraction we start at the right-hand side.

Year 3



Children could draw place value counters.

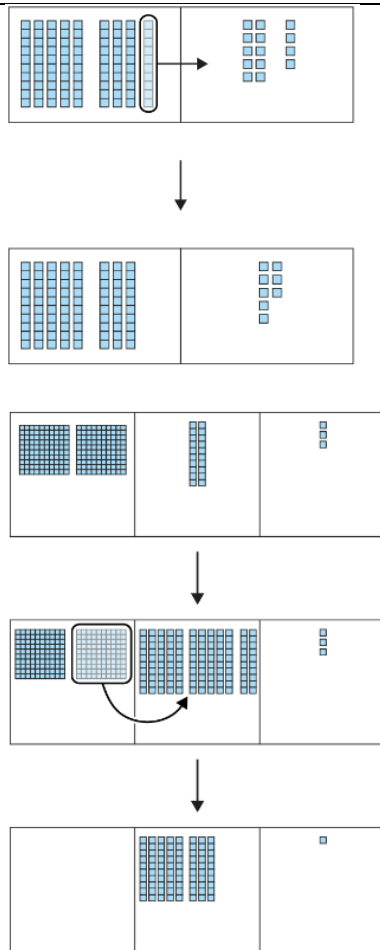


$$\begin{array}{r} 65 \\ - 23 \\ \hline 42 \end{array}$$

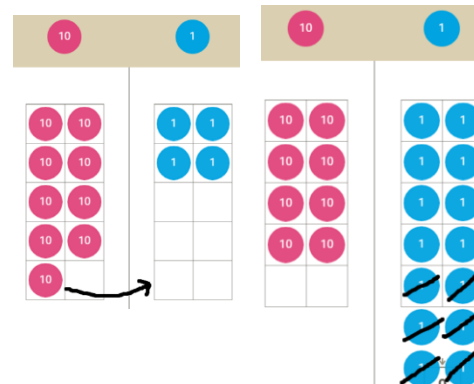
$$\begin{array}{r} 462 \\ - 251 \\ \hline \end{array}$$

If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.

Year 3



Children could draw place value counters.



$$\begin{array}{r|l} 10s & 1s \\ \hline 9 & 14 \\ - & 6 \\ \hline \end{array}$$

$$\begin{array}{r|l} 10s & 1s \\ \hline 9 & 14 \\ - & 6 \\ \hline 8 & 8 \end{array}$$

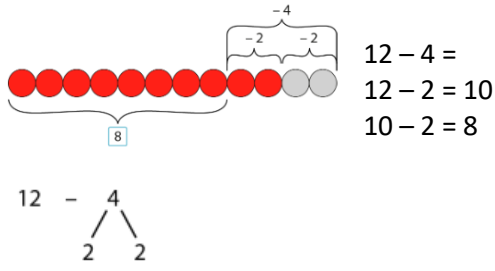
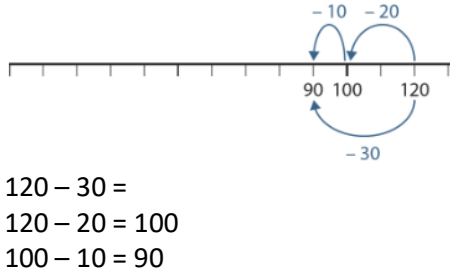
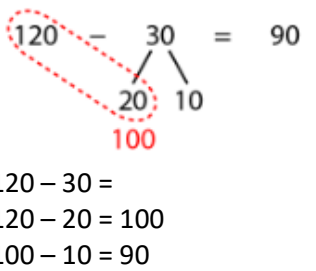
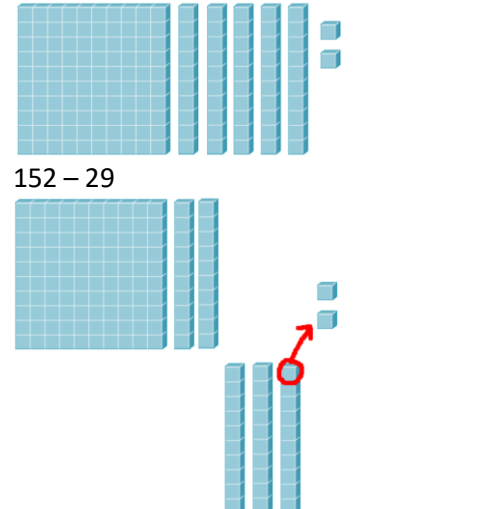
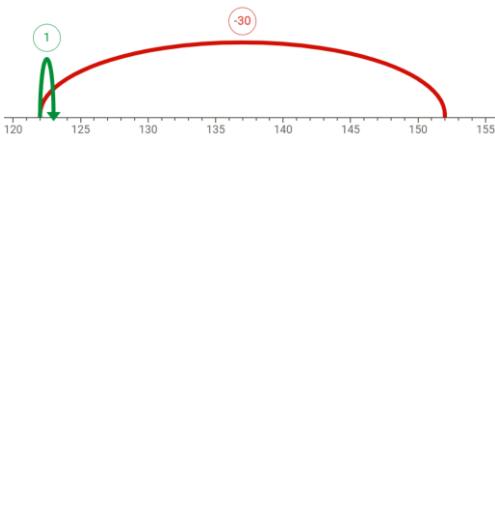
$$\begin{array}{r|l|l} 100s & 10s & 1s \\ \hline 2 & 2 & 3 \\ - 1 & 4 & 2 \\ \hline \end{array}$$

$$\begin{array}{r|l|l} 100s & 10s & 1s \\ \hline 2 & 12 & 3 \\ - 1 & 4 & 2 \\ \hline \end{array}$$

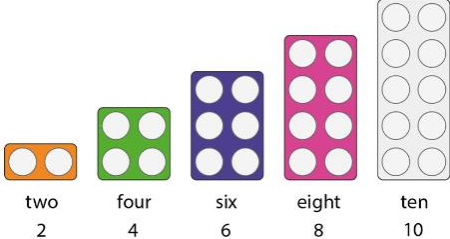
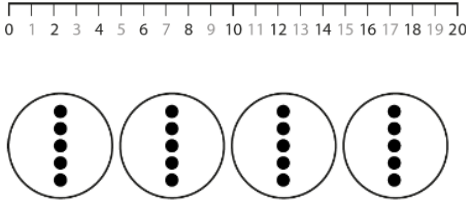


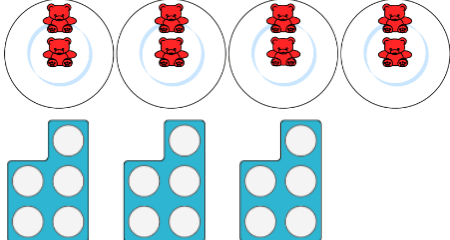
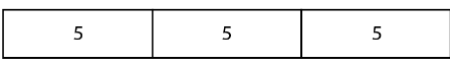

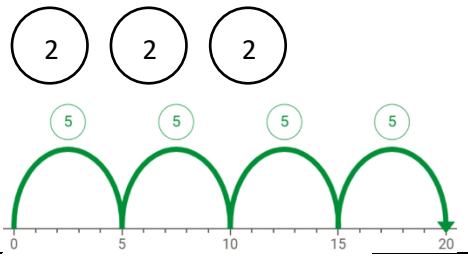
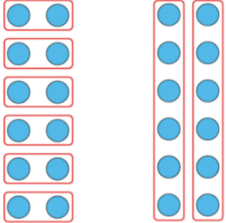
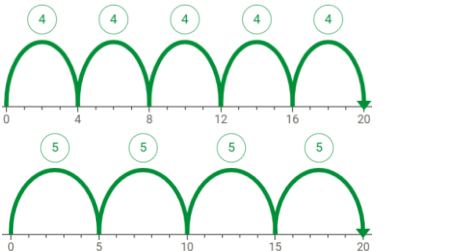
$$\begin{array}{r|l|l} 100s & 10s & 1s \\ \hline 2 & 12 & 3 \\ - 1 & 4 & 2 \\ \hline 0 & 8 & 1 \end{array}$$

<p>If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.</p> <p>Year 4</p>	See Year 3 examples	See Year 3 examples	$ \begin{array}{r} \overset{5}{\cancel{6}}, \overset{14}{\cancel{5}}, \overset{12}{\cancel{3}}, 8 \\ - 2, 7 \ 8 \ 9 \\ \hline 3, 7 \ 4 \ 9 \end{array} $ $ \begin{array}{r} \pounds \ 2 \ \overset{8}{\cancel{9}} \cdot \overset{14}{\cancel{5}} \ 0 \\ - \pounds \ 1 \ 8 \cdot 9 \ 4 \\ \hline \pounds \ 1 \ 0 \cdot 5 \ 6 \end{array} $
<p>If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.</p> <p>Years 5 and 6</p>	See Year 3 examples	See Year 3 examples	As in Year 4 but using numbers with more than 4 digits

Subtraction – Key mental strategies for Key Stage 2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Bridging through a multiple of 10, 100, etc Years 3, 4, 5 and 6	 $12 - 4 =$ $12 - 2 = 10$ $10 - 2 = 8$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$
Compensating – rounding to the nearest multiple 10, 100, etc and adjusting Years 3, 4, 5 and 6	 $152 - 29$	 $152 - 30 = 122$ $122 + 1 = 123$	$152 - 30 = 122$ $122 + 1 = 123$

Multiplication

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p>Year R/1</p>			<p>10, 20, 30, ...</p>
<p>There are __ coins.</p> <p>Each coin has a value of __p.</p> <p>This is __p.</p> <p>Year 1</p>	 <p>Representing each group by one object</p>		<p>Five 2p coins = 10p</p>
<p>There are __ in each group.</p> <p>There are __ groups.</p> <p>There are __ in a group and __ groups.</p> <p>Year 2</p>			<p>$2 + 2 + 2 + 2 = 8$</p> <p>$2 \times 4 = 8$</p> <p>$5 + 5 + 5 = 15$</p> <p>$5 \times 3 = 15$</p>
<p>Factor times factor is equal to the product.</p> <p>The product is equal to factor times factor.</p> <p>Year 2</p>	 <p>Unitising equal groups – representing each group by one object</p>		<p>$2 \times 3 = 6$</p> <p>$6 = 2 \times 3$</p>
<p>__ times __ can represent __ in a group and __ groups.</p> <p>It can also represent __ groups of __.</p> <p>Multiplication is commutative.</p> <p>Year 2</p>			<p>$2 \times 5 = 5 \times 2$</p>

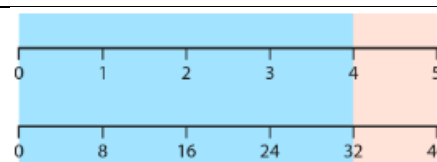
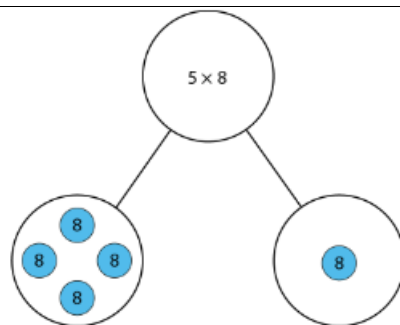
__ is equal to __ plus __, so __ times __ is equal to __ times __ plus __ times __.

__ is equal to __ minus __, so __ times __ is equal to __ times __ minus __ times __.

Multiplication is distributive.

(NCETM Year 4 unit 2.10)

Year 3



$$\begin{aligned} 5 &= 4 + 1 \\ 5 \times 8 &= 4 \times 8 + 1 \times 8 \\ &= 32 + 8 \\ &= 40 \end{aligned}$$

$$\begin{aligned} 4 &= 5 - 1 \\ 4 \times 8 &= 5 \times 8 - 1 \times 8 \\ &= 40 - 8 \\ &= 32 \end{aligned}$$

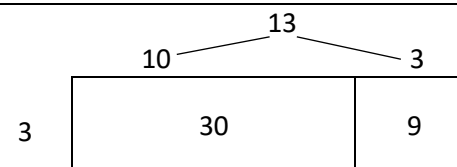
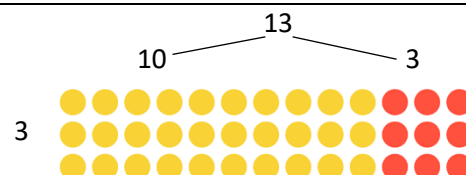
__ is equal to __ plus __, so __ times __ is equal to __ times __ plus __ times __.

__ is equal to __ minus __, so __ times __ is equal to __ times __ minus __ times __.

Multiplication is distributive.

(NCETM Year 4 unit 2.10)

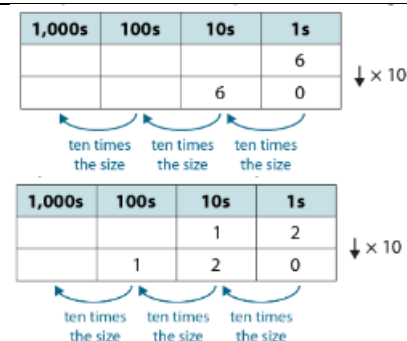
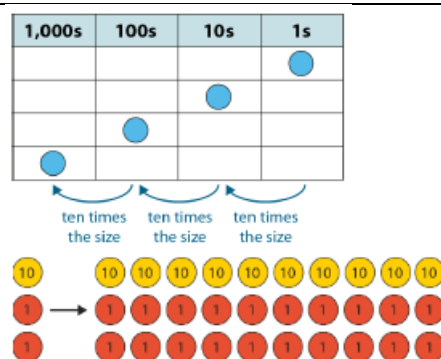
Year 3



$$\begin{aligned} 3 \times 13 &= 3 \times 10 + 3 \times 3 \\ &= 30 + 9 \\ &= 39 \end{aligned}$$

To multiply a whole number by 10, place a zero after the final digit of that number.

Year 4

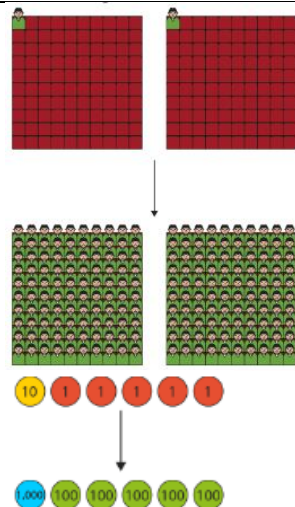


$$6 \times 10 = 60$$

$$12 \times 10 = 120$$

All multiples of 100 have both a tens and ones digit of 0.
When a number is multiplied by 100, the product is a multiple of 100.

Year 4



1,000s	100s	10s	1s
			6
	6	0	0

↓ × 100

100 times the size

1,000s	100s	10s	1s
		1	5
1	5	0	0

↓ × 100

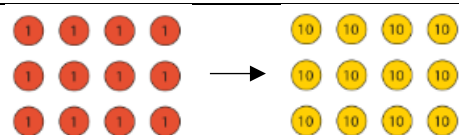
100 times the size 100 times the size

$2 \times 100 = 200$
There are 100 times as many people as before.

$$15 \times 100 = 1500$$

If one factor is made ten times the size, the product will be ten times the size.

Year 4



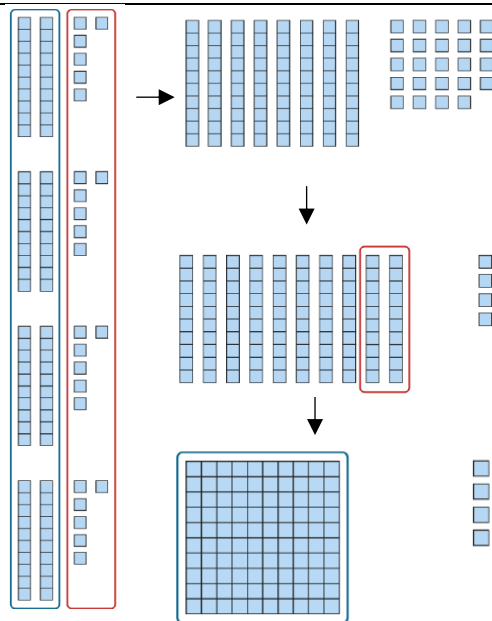
$$\begin{array}{l} 2 \times 3 = 6 \\ \times 10 \downarrow \quad \times 10 \downarrow \\ 2 \times 30 = 60 \end{array}$$

$$4 \times 3 = 12 \text{ so } 4 \times 30 = 120$$

If there are ten or more ones, we must regroup the ones into tens and ones.
If there are ten or more tens, we must regroup the tens into hundreds and tens.

Multiplication is distributive.

Year 4



$$\begin{array}{r} 84 \times 6 = 504 \\ \begin{array}{r} 80 \\ 4 \end{array} \end{array}$$

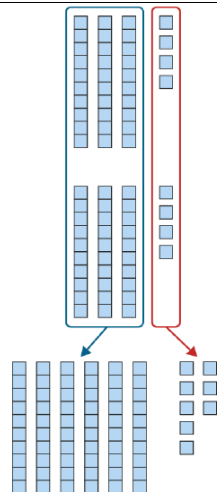
$$\begin{array}{l} 80 \times 6 = 480 \\ 4 \times 6 = 24 \\ 480 + 24 = 504 \end{array}$$

$$\begin{array}{l} 84 \times 6 = 80 \times 6 + 4 \times 6 \\ = 480 + 24 \\ = 504 \end{array}$$

We work from the least significant digit, on the right, to the most significant digit, on the left.

Multiplication is distributive.

Year 4



$$34 \times 2 = 60 + 8 = 68$$

10s	1s
3	4
×	2
	8
6	0
6	8

$2 \times 4 \text{ ones} = 8 \text{ ones}$

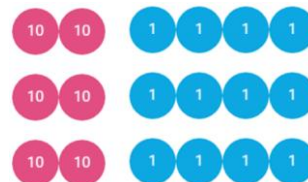
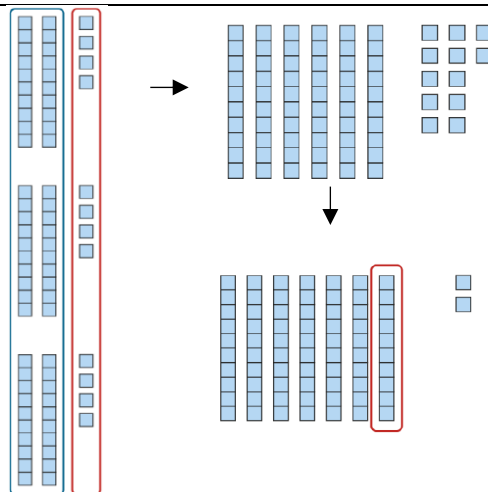
$2 \times 3 \text{ tens} = 6 \text{ tens}$

2	1
×	4
8	4

If there are ten or more ones, we must regroup the ones into tens and ones.
If there are ten or more tens, we must regroup the tens into hundreds and tens.

Multiplication is distributive.

Year 4



$$24 \times 3 = 60 + 12 = 72$$

10s	1s
2	4
×	3
1	2
6	0
7	2

$3 \times 4 \text{ ones} = 12 \text{ ones} = 1 \text{ ten} + 2 \text{ ones}$

$3 \times 2 \text{ tens} = 6 \text{ tens}$

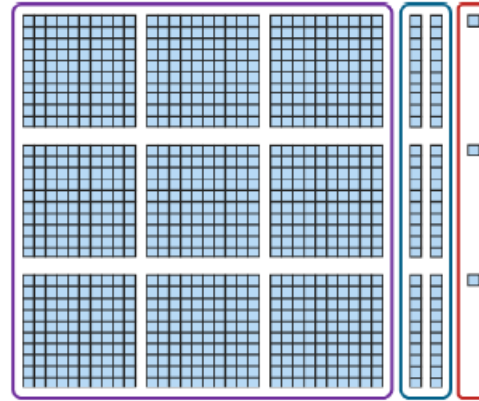
1	8
×	5
9	0
4	

3	8	
×	4	
1	5	2
3		

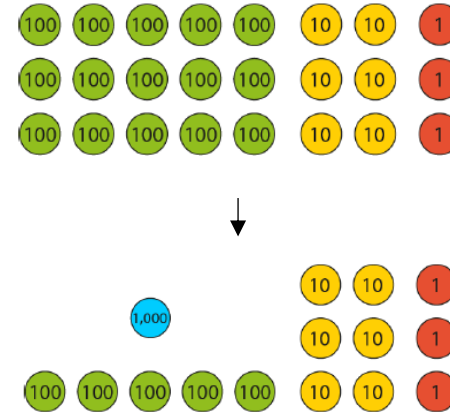
If there are ten or more ones, we must regroup the ones into tens and ones.
 If there are ten or more tens, we must regroup the tens into hundreds and tens.
 If there are ten or more hundreds, we must regroup the hundreds into thousands and hundred.

Multiplication is distributive.

Year 4



$$321 \times 3 = 963$$



$$521 \times 3 = 1000 + 500 + 60 + 3 = 1563$$

	100s	10s	1s
3	2	1	
×			3
		6	0
	9	0	0
	9	6	3

$3 \times 1 \text{ ones} = 3 \text{ ones}$
 $3 \times 2 \text{ tens} = 6 \text{ tens}$
 $3 \times 3 \text{ hundreds} = 9 \text{ hundreds}$

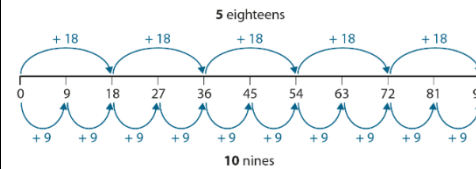
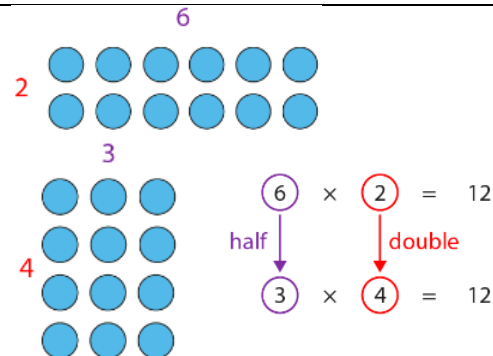
	1,000s	100s	10s	1s
		5	2	1
×				3
			6	0
	1	5	0	0
	1	5	6	3

	3	6	7
×			4
	1	4	6
	2	2	

If there is a multiplicative increase in one factor and a multiplicative decrease in the other, the product remains the same.

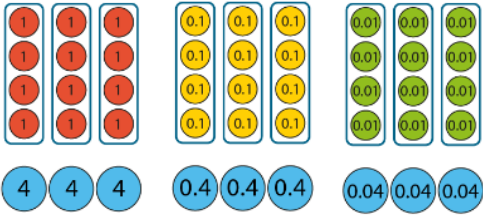
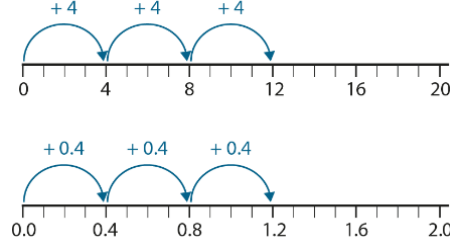
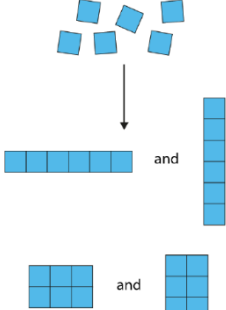
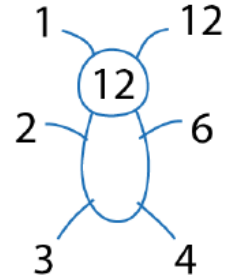
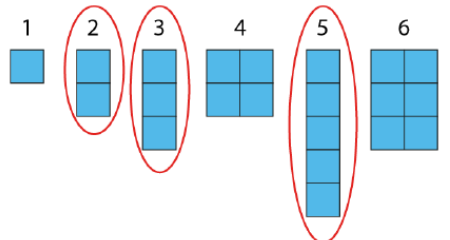
If I multiply one factor by __, I must divide the other factor by __ for the product to remain the same.

Year 5 and 6



$$2 \times 9 = 18$$

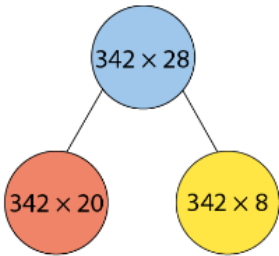
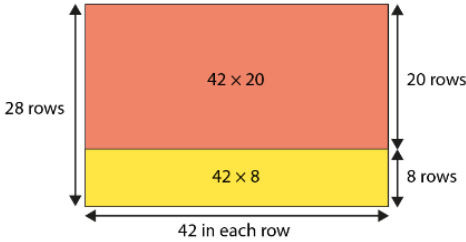
$$3 \times 6 = 18$$

<p>If one factor is made one tenth of the size, the product will be one tenth of the size.</p> <p>If one factor is made one hundredth of the size, the product will be one hundredth of the size.</p> <p>I move the digits of the number I am multiplying ___ places to the left until I get a whole number; then I multiply; then I move the digits of the product ___ places to the right.</p> <p>Year 5</p>	 <p> $4 \times 3 = 12$ $0.4 \times 3 = 1.2$ $0.04 \times 3 = 0.12$ </p>		$\begin{array}{r} 456 \\ \times \quad 4 \\ \hline 1824 \\ 22 \end{array}$ $\begin{array}{r} 4.56 \\ \times \quad 4 \\ \hline 18.24 \\ 22 \end{array}$
<p>Numbers that have more than two factors are composite numbers.</p> <p>Year 5</p>	 <p>Factors of 6 are 1, 2, 3 and 6.</p>	 <p>Factor bugs</p>	<p>Factors of 6 are 1, 2, 3 and 6.</p>
<p>Numbers that have only two factors are prime numbers.</p> <p>Year 5</p>			<p>17 is a prime number because its only factors are 1 and 17.</p>

To multiply two two-digit numbers, first multiply by the ones, then multiply by the tens, then add them together.

To multiply a three-digit number by a two-digit number, first multiply by the ones, then multiply by the tens, then add them together.

Year 6



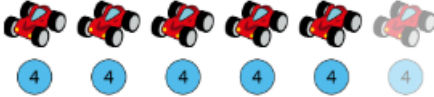
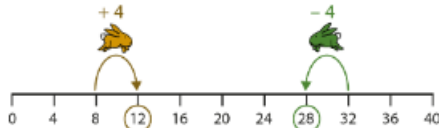
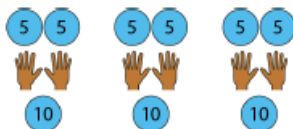
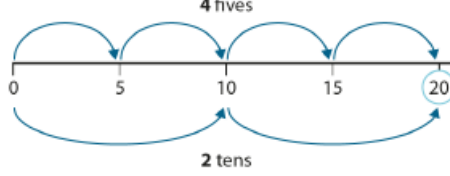
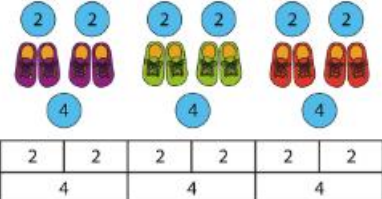
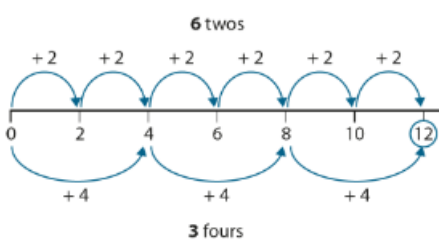
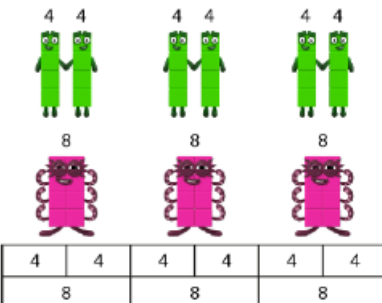
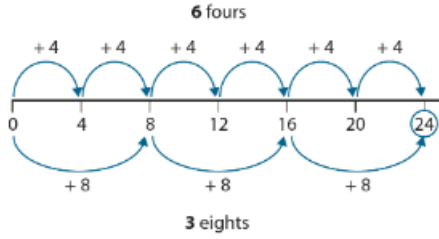
	100s	10s	1s
×		2	7
		2	3
		8	1
	5	4	0
	6	2	1
	1		

27 × 3

27 × 20

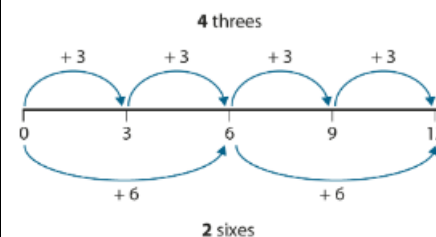
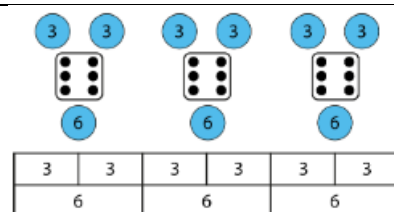
	3	1	2
×		2	8
	2	4	9
	6	2	4
	8	7	3
			6
			1

Multiplication – Key mental strategies for Key Stage 2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>Adjacent multiples of ___ have a difference of ___.</p> <p>Year 3 onwards</p>			$4 \times 6 = 4 \times 5 + 4$ $4 \times 9 = 4 \times 10 - 4$
<p>Products in the 10 times table are double the products in the 5 times table. Products in the 5 times table are half of the products in the 10 times table.</p> <p>(NCETM Year 2 unit 2.5)</p> <p>Year 3 onwards</p>			$5 \times 4 = 10 \times 2$
<p>Products in the 4 times table are double the products in the 2 times table. Products in the 2 times table are half of the products in the 4 times table.</p> <p>Year 3 onwards</p>			$2 \times 6 = 4 \times 3$
<p>Products in the 8 times table are double the products in the 4 times table. Products in the 4 times table are half of the products in the 8 times table.</p> <p>Year 3 onwards</p>			$4 \times 6 = 8 \times 3$

Products in the 6 times table are double the products in the 3 times table.
Products in the 3 times table are half of the products in the 6 times table.

Year 3 onwards

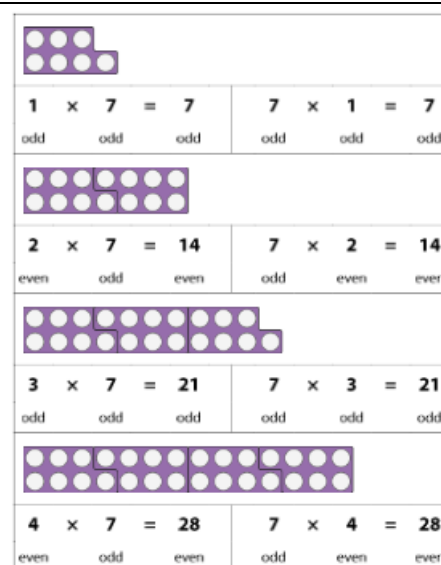


$$3 \times 4 = 6 \times 2$$

When both factors are odd, the product is odd.
When one factor is odd and the other factor is even, the product is even.

(NCETM Year 3 unit 2.9)

Year 3 onwards

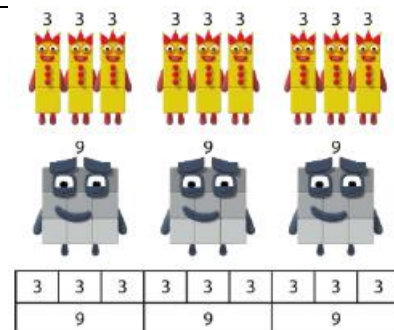


$$\text{odd} \times \text{odd} = \text{odd}$$

$$\begin{aligned} \text{odd} \times \text{even} &= \text{even} \\ \text{even} \times \text{odd} &= \text{even} \end{aligned}$$

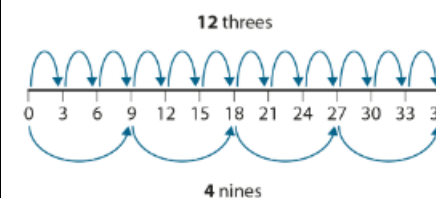
$$\text{even} \times \text{even} = \text{even}$$

Products in the 9 times table are triple the products in the 3 times table.

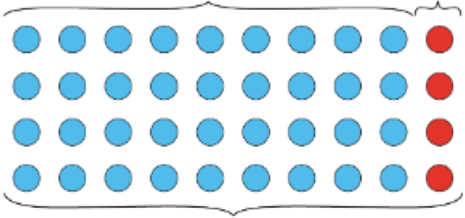
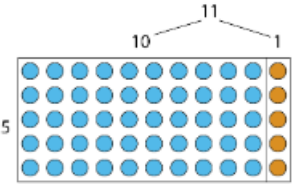
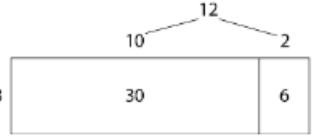


$$9 \times 4$$


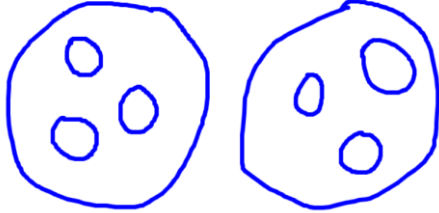

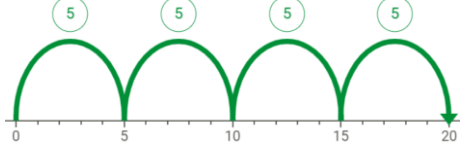

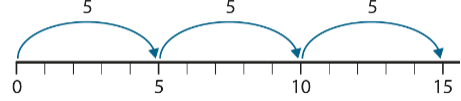
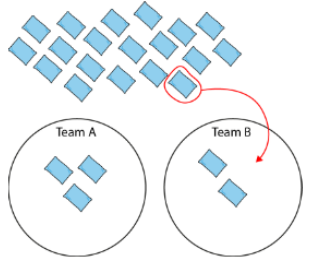
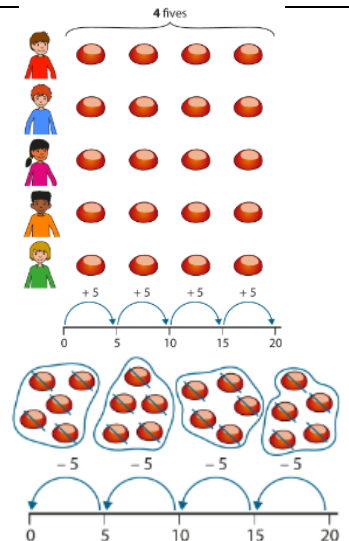
$$1 \times 4$$

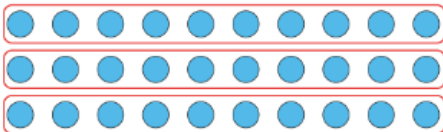
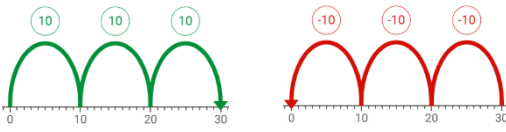
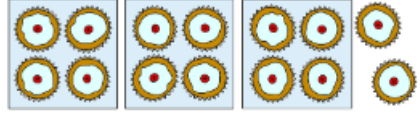
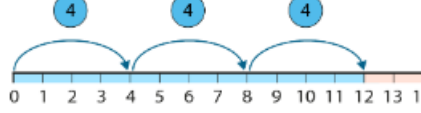
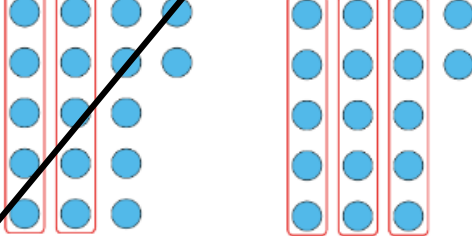
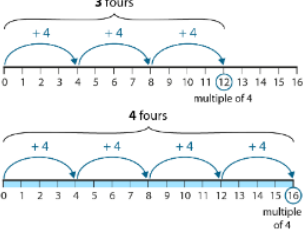
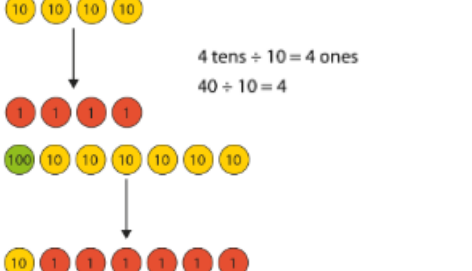
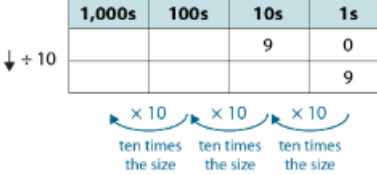


$$3 \times 12 = 9 \times 4$$

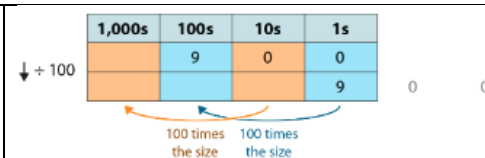
<p>Products in the 10 times table can be used to find products in the 9 times table.</p> <p>(NCETM Year 3 unit 2.8)</p> <p>Year 4 onwards</p>	 <p style="text-align: center;">10×4</p>		$9 \times 4 = 10 \times 4 - 1 \times 4$
<p>Products in the 10 times table can be used to find products in the 11 times table and 12 times table.</p> <p>Year 4 onwards</p>			$ \begin{aligned} 12 \times 3 &= 10 \times 3 + 2 \times 3 \\ &= 30 + 6 \\ &= 36 \end{aligned} $

Division

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p>Year R/1</p>			<p>6 biscuits shared between 2 children gives 3 biscuits each.</p>
<p>The ____ costs __p.</p> <p>Each coin has a value of __p.</p> <p>So I need __ coins.</p> <p>Year 1</p>			<p>Five 2p coins = 10p</p>
<p>__ is divided into groups of __.</p> <p>There are __ groups.</p> <p>We can skip count using the divisor to find the quotient.</p> <p>Year 2</p>			<p>$5 + 5 + 5 = 15$ $15 \div 5 = 3$</p>
<p>__ divided between __ is equal to __ each.</p> <p>We can skip count using the divisor to find the quotient.</p> <p>Year 2</p>			<p>One 5 is 1 each. That's 5. Two 5s is 2 each. That's 10. $10 \div 5 = 2$</p> <p>Dividend divided by the divisor equals the quotient.</p>

<p>Ten times __ is equal to __ so __ divided into groups of ten is __.</p> <p>If the divisor is __, we can use the __ times table to find the quotient.</p> <p>Year 2</p>	 <p>30 represents the total number of counters.</p> <p>10 represents the number in each group.</p> <p>3 represents the number of groups.</p>		$10 \times 3 = 30$ $3 \times 10 = 30$ $30 \div 10 = 3$
<p>__ is divided into groups of __. There are __ groups and a remainder of __.</p> <p>(NCETM Year 4 unit 2.12)</p> <p>Year 3</p>			$14 = 4 \times 3 + 2$ $14 \div 4 = 3 \text{ r } 2$
<p>__ is a multiple of __ so when it is divided into groups of __, there is no remainder.</p> <p>The remainder is always less than the divisor.</p> <p>(NCETM Year 4 unit 2.12)</p> <p>Year 3 or 4?</p>			<p>$17 \div 5 = 2 \text{ r } 7$ is incorrect because 7 is greater than 5.</p> <p>$17 \div 5 = 3 \text{ r } 2$</p>
<p>To divide a multiple of ten by 10 move the digits one place to the right and remove the zero.</p> <p>Year 4</p>	 <p>4 tens $\div 10 = 4$ ones $40 \div 10 = 4$</p>	 <p>$\downarrow \div 10$</p> <p>$\times 10$ ten times the size $\times 10$ ten times the size $\times 10$ ten times the size</p>	$90 \div 10 = 9$ $150 \div 10 = 15$

Year 4

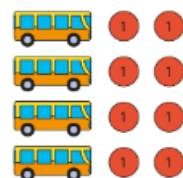


$900 \div 100 = 9$

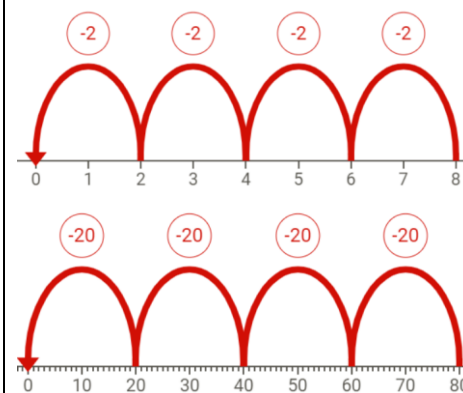
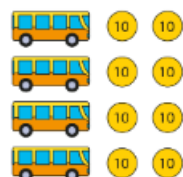
$$1500 \div 100 = 15$$

Year 4

$$8 \div 4 = 2$$

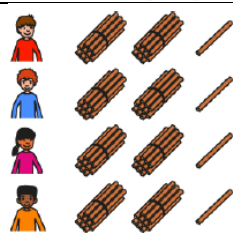


$$80 \div 4 = 20$$

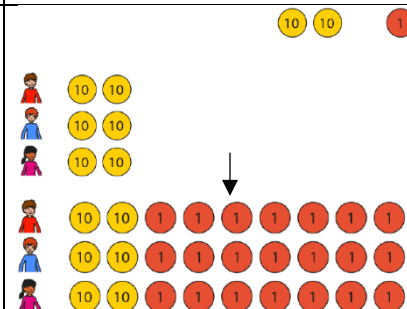


$$\begin{array}{ccccc} 12 & \div & 3 & = & 4 \\ \times 10 \downarrow & & & & \downarrow \times 10 \\ 120 & \div & 3 & = & 40 \end{array}$$

Year 4



$$84 \div 4 = 21$$

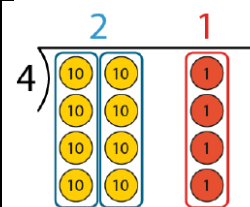
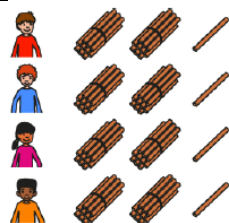


8 tens	÷	4	=	2 tens
4 ones	÷	4	=	1 one
84	÷	4	=	21

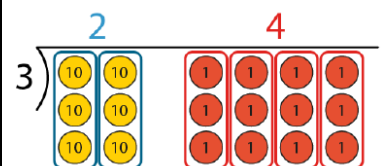
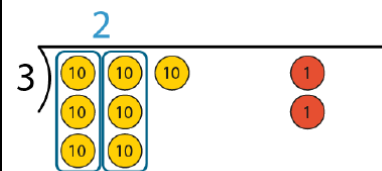
6 tens	÷	3	=	2 tens
21 ones	÷	3	=	7 ones
81	÷	3	=	27

If dividing the tens gives a remainder of one or more tens, we must exchange the remaining tens for ones.

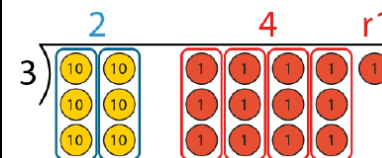
Year 4



$$72 \div 3 = 24$$



$$73 \div 3 = 24 \text{ r } 1$$



$$\begin{array}{r} 10\text{s} \quad 1\text{s} \\ 4 \overline{) 8 \quad 4} \\ \underline{8 \quad 4} \\ 0 \end{array}$$

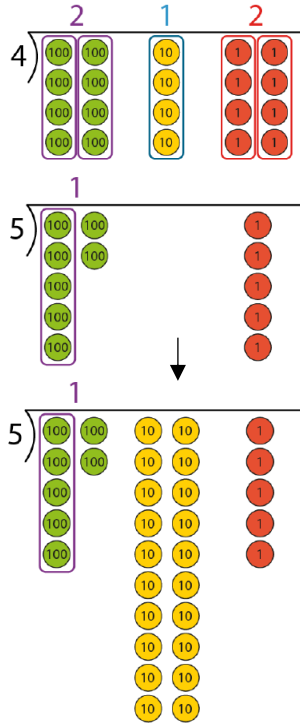
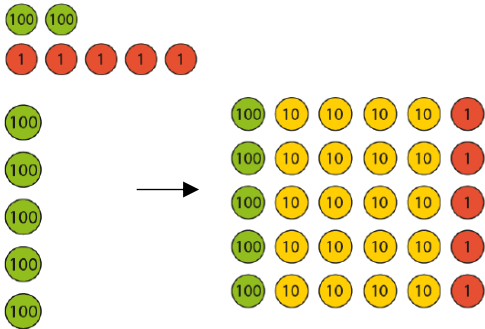
8 tens \div 4 = 2 tens
4 ones \div 4 = 1 one

$$\begin{array}{r} 2 \quad 4 \\ 3 \overline{) 7 \quad 1 \quad 2} \\ \underline{6 \quad 1 \quad 2} \\ 0 \end{array}$$

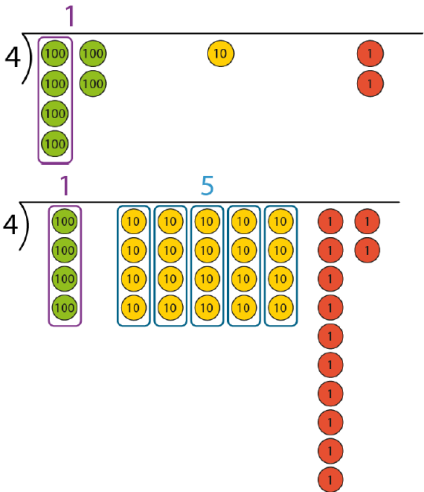
$$\begin{array}{r} 2 \quad 4 \text{ r } 1 \\ 3 \overline{) 7 \quad 1 \quad 3} \\ \underline{6 \quad 1 \quad 3} \\ 0 \end{array}$$

If dividing the hundreds gives a remainder of one or more hundreds, we must exchange the remaining hundreds for tens.

Year 4



$$612 \div 4 = 153$$



$$\begin{array}{r} 212 \\ 4 \overline{) 848} \end{array}$$

$$\begin{array}{r} 141 \\ 5 \overline{) 7205} \end{array}$$

$$\begin{array}{r} 153 \\ 4 \overline{) 6212} \end{array}$$

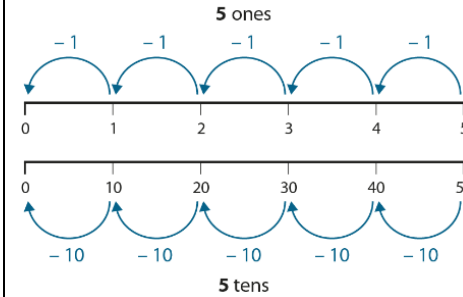
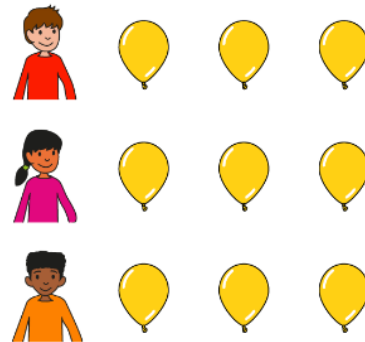
If there is a multiplicative change to the dividend factor and a corresponding change to the divisor, the quotient remains the same.

If I multiply the dividend by __, I must multiply the divisor by __ for the quotient to remain the same.

Year 5 and 6



$$\begin{array}{c} 3 \div 1 = 3 \\ \times 3 \quad \times 3 \\ \hline 9 \div 3 = 3 \end{array}$$



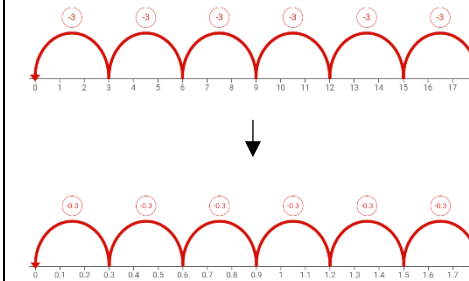
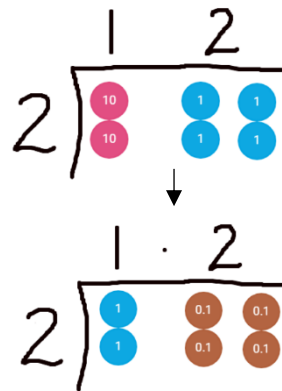
$$\begin{array}{c} 40 \div 10 = 4 \\ \times 10 \quad \times 10 \\ \hline 400 \div 100 = 4 \end{array}$$

If the dividend is made one tenth of the size, the quotient will be one tenth of the size.

If the dividend is made one hundredth of the size, the quotient will be one hundredth of the size.

I move the digits of the dividend __ places to the left until I get a whole number; then I divide; then I move the digits of the quotient __ places to the right.

Year 5 onwards

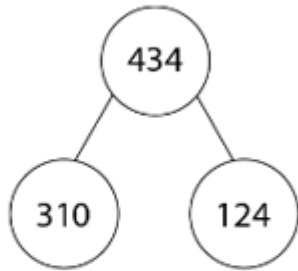


$$\begin{array}{c} 0.85 \div 5 = 0.17 \\ \times 100 \quad \div 100 \\ \hline 85 \div 5 = 17 \end{array}$$

$$\begin{array}{r} 0 \ 5 \ 1 \\ 5 \overline{) 2 \ 2 \ 5 \ 5} \end{array} \rightarrow \begin{array}{r} 0 \ 5 \ . \ 1 \\ 5 \overline{) 2 \ 2 \ 5 \ . \ 5} \end{array}$$

Any two-, three- or four-digit dividend can be divided by a two-digit divisor using skip-counting in multiples of the divisor, or by short division.

Year 6

Partitioning	Short division
 $\begin{array}{r} 310 \div 31 = 10 \\ 124 \div 31 = 4 \\ \hline 434 \div 31 = 14 \end{array}$	$\begin{array}{r} 0 \quad 1 \quad 4 \\ 31 \overline{) 4 \quad 3 \quad 12 \quad 4} \end{array}$

Where there is a remainder, the result can be expressed as a whole-number quotient with a whole-number remainder, a whole-number quotient with a proper-fraction remainder, or as a decimal-fraction quotient.

Year 6

$\begin{array}{r} 2 \quad 3 \quad r9 \\ 15 \overline{) 3 \quad 5 \quad 4} \end{array}$	$\begin{array}{r} 2 \quad 3 \quad \frac{9}{15} \\ 15 \overline{) 3 \quad 5 \quad 4} \end{array}$	$\begin{array}{r} 2 \quad 3 \quad . \quad 6 \\ 15 \overline{) 3 \quad 5 \quad 4 \quad . \quad 0} \end{array}$
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